KCATM 2012 HIGH SCHOOL MATHLETICS

Team #_____

Problem #1

Question #1: Find the area of the annulus formed when $(x-3)^2 + (y-1)^2 = 36$ is placed inside $x^2 - 6x + y^2 - 2y = 71$. Express your answer in terms of pi.

Problem #2

<u>Question #2</u>: Find the area of the triangle with vertices at (-1, 4), (5, 12) and (5, 6). Give an exact answer.

Problem #3

1 minute, 1 point

Question #3: Find the number of ways to arrange the letters in the word MISSISSIPPI?

Problem #4

Question #4: Solve the system and give all solutions: $\begin{cases} y = \frac{1}{2}x^2 - 5\\ x^2 + y^2 = 25 \end{cases}$

Problem #5

Question #5: At the University of Wisconsin during home football games, the mascot does pushups corresponding to the team's score. For example, if Wisconsin's first score is a touchdown, the mascot does 7 pushups. If Wisconsin's second score is a field goal (bringing their point total to 10), the mascot does an additional 10 pushups. (So, he has now done 17 total pushups.) Determine how many total pushups the mascot will do given the sequence of scores below:

- 1st possession field goal (3 total points)
 2nd possession field goal (3 more points)
 3rd possession touchdown (7 more points)
 4th possession field goal (3 more points)
 5th possession touchdown (7 more points)
 6th possession touchdown (7 more points)
- 7th possession touchdown (7 more points)

Problem #6

Problem #6: Solve for n (n must be a positive integer): $\frac{(n+2)!}{n!2!} = 465$

Problem #7

1 minute, 1 point

Problem #7: Find the sum of the first 200 integers.

Problem #8

Question #8: How many integers lie in the domain of $f(x) = \csc\left(\frac{\pi}{2}x\right)\sqrt{16-x^2}$?

Problem #9

<u>Question #9:</u> Suppose $\log(2) = A$, $\log(3) = B$, and $\log(5) = C$. Express $\log\left(\frac{2\sqrt[3]{9}}{25}\right)$ in terms of A, B and C.

Problem #10

1 minute, 1 point

<u>Question #10:</u> Evaluate the series:

25 + 20 + 14 + 11.2 + ...

Problem #11

Question #11: If x + 3y + 5z = 200 and x + 4y + 7z = 225, then what does x + y + z equal?

Problem #12

Question #12: Joan can mow a lawn in 90 minutes, and Sylvia can mow the same lawn in 60 minutes, how long will it take them working together?

Problem #13

Question #13: A car travels up a hill with an average speed of 60 miles per hour. With what average speed does it have to travel down the hill to have an average speed of 70 miles per hour for the entire trip?

Problem #14

Question #14: A class consists of 28 students. The class has 16 girls and 12 boys. The teacher is looking to randomly construct a student committee consisting of 7 students. Find the probability that the randomly selected committee consists of <u>exactly</u> 3 girls and 4 boys. Round your answer to the nearest percent.

Problem #15

<u>Question #15:</u> A six-sided die is constructed so that there is a 1/21 chance of rolling a 1, a 2/21 chance of rolling a 2, a 3/21 chance of rolling a 3, a 4/21 chance of rolling a 4, a 5/21 chance of rolling a 5, and a 6/21 chance of rolling a 6. The six-sided die is rolled twice. Find the probability that the sum of the two rolls is exactly 7. Express your answer as a fraction in lowest terms.

Problem #16

<u>Question #16:</u> A certain function f satisfies f(x) + 2f(6 - x) = x for all real numbers x. Find the value of f(1).